# SKH St. Simon's Lui Ming Choi Secondary School Form 2 Mathematics Tiered Assignment Chapter 2 Identities and Factoriztion



1. Prove that the equation 3(2x - 4) = 2(-6 + 3x) is an identity.

2. Determine whether each of the following equations is an identity.

(a) 
$$(x+1)(2x-1) = 2x(x+1) + (x-1)$$
 (b)  $2x(x-1) - x - 5 = (2x-5)(x+1)$ 

3. If  $(x-2)(x+5) \equiv x^2 + Px + Q$ , where *P* and *Q* are constants, find *P* and *Q*.

- 4. Expand the following.
  - (a) (x-5)(x+5)
  - (b) (6-x)(6+x)
  - (c) (7+y)(7-y)
  - (d) (2x+7)(2x-7)
  - (e) (3x-4)(3x+4)
  - (f) (4x+5y)(4x-5y)

- (g)  $(k+3)^2$
- (h)  $(1+7n)^2$
- (i)  $(m-8)^2$
- (j)  $(3p+1)^2$ (k)  $(5m+2n)^2$

5. Factorize the following expressions.

(a) 9c + 9d

- (b) -ab 2a
- (c) 3a + 2ab ac

(d) 3kx - 9ky - 15kz

- (e)  $8a^3 + 20ab^2 12a$
- (f)  $24x^2y^3 40xy^3 56x^2y^2$

- 6. Expand the following.
  - (a) (-4a-3)(-4a+3)
  - (b) (-h+3k)(3k+h)
  - (c) 2(3m-1)(1+3m)
  - (d) 3(3x+5y)(3x-5y)
  - (e) (3-2xy)(3+2xy)
  - (f)  $(4a+b^2)(4a-b^2)$
  - (g)  $(-5-y^3)(-5+y^3)$

- (h) (mn 4)(-mn 4)
- (i)  $(-3-5n)^2$
- (j)  $(-8a+5b)^2$
- (k)  $3(2x-y)^2$
- (1)  $\left(x-\frac{y}{8}\right)^2$

- 7. Factorize the following expressions.
  - (a)  $3m^2n + m^2 3n^2 n$
  - (b)  $4p^2 3q 2pq + 6p$
  - (c)  $-12x^2 4xy 18x 6y$

8. Without using a calculator, find the values of the following expressions. (a)  $77^2 - 23^2$  (b)  $298 \times 302$ 

9. Without using a calculator, find the values of the following expressions.
(a) 205<sup>2</sup>
(b) 47<sup>2</sup>

#### Level 2

10. Factorize the following expressions.

(a) 2ax + 4bx - 2cx + ay + 2by - cy

(b) 8ax + 6bx - 4ay - 3by + 12a + 9b

11.

- (a) Expand  $(x + 3y)^2$ .
- (b) Hence, expand (x + 3y 2)(x + 3y + 2).

12. Expand the following.

- (a) Expand (2x + 9y)(2x 9y).
- (b) Using the result of (a), expand  $\left(\frac{2x}{3}+3y\right)\left(\frac{x}{3}-\frac{3y}{2}\right)$ .

13. If  $(x + 3M)(2x - 1) + 4 \equiv x(2x - 7) + N$ , where *M* and *N* are constants, find *M* and *N*.

# SKH St. Simon's Lui Ming Choi Secondary School Form 2 Mathematics Tiered Assignment Chapter 3 Formulae

| Name: | Class: | ( ) | Date: |  |
|-------|--------|-----|-------|--|
|       | _      |     | _     |  |

#### Level 1:

1. Simplify

(a) 
$$\frac{4a^2b^3}{2ab}$$
  
(b)  $8m - 12m^2$ 

(b) 
$$\frac{6m^2}{12mn}$$

(c) 
$$\frac{13ax - 3ay}{20bx - 4by}$$

(d) 
$$\frac{8b-2a}{a^2-4ab}$$

(e) 
$$\frac{yx-2x+y-2}{y-2}$$

## 2. Simplify

(a) 
$$\frac{4m}{n} \times \frac{5n}{8m}$$
  
(b)  $\frac{q}{5p} \div \frac{q^2}{10}$   
(c)  $\frac{8m^4}{r} \times \frac{n}{16m} \div \frac{3n}{r^2}$   
(d)  $\frac{bm-bn}{ax} \times \frac{3c^2}{cn-cm}$ 

## 3. Simplify

(a) 
$$\frac{5n}{3m} + \frac{n}{3m}$$

(b) 
$$\frac{6x}{3x-4y} - \frac{8y}{3x-4y}$$

(c) 
$$\frac{4}{5n} - \frac{1}{m}$$

(d) 
$$\frac{2y}{3x} + \frac{y}{2x} - \frac{11y}{12x}$$

(e) 
$$\frac{2m}{3m-4n} - \frac{n}{2(4n-3m)}$$
  
(f)  $1 + \frac{1-4y}{3y}$ 

(g) 
$$\frac{6x}{2x+5y} - 2$$

4. Given that T = t + 273.15, find the value of T if t = 32.

5. Consider the formula  $Q = y^4$ . If y = 3, find Q.

6. Consider the formula  $y = \frac{x(x+1)}{2}$ . If x = -11, find y.

7. Given that  $v^2 = u^2 + 2as$ , find the value of a if v = 20, u = 10 and s = 15.

8. Consider the formula y = kx + b. If y = 17, k = -3 and b = 5, find x.

9. Change the subject of each of the following formulae to the letter in the square brackets.

(a) 
$$K = 2pt$$
 [p]  
(b)  $5 + \frac{x}{y} = z$  [x]

10. Make *y* the subject of the formula y - c = m(6 - y).

### Level 2:

11. Simplify

(a) 
$$\frac{3}{a-2b} + \frac{2}{2b-a}$$
  
(b)  $\frac{2x}{2x-1} - \frac{x}{x+3}$ 

12. The perimeter *P* m of a regular *n*-sided polygon of side *a* m can be calculated by the formula P = na. What is the length of a side of a pool in the shape of a regular octagon of perimeter 40 m?

13. A pack consists of two pieces of chocolate in the shape of hemispheres as shown below. The diameters of their bases are *D* cm and *d* cm respectively. The total volume *V* cm<sup>3</sup> of chocolate in the pack can be calculated by the formula  $V = \frac{1}{12} \pi (D^3 + d^3)$ . If D = 4 and d = 2, is 50 cm<sup>3</sup> of chocolate enough to make 3 such packs? Explain your answer. (*Take*  $\pi = 3.14$ .)



14. Make x the subject of the formula  $\frac{1}{x} + \frac{2}{y} = \frac{r}{s}$ .

- 15. The length, the width and the height of a gold brick in the shape of a rectangular block are  $\ell$  cm, w cm and h cm respectively. The weight M g of the gold brick can be calculated by the formula  $M = 19.3\ell wh$ .
  - (a) Express h in terms of M,  $\ell$  and w.
  - (b) It is known that a gold brick in the shape of a rectangular block weighs 900 g. If its length is 12 cm and its width is 5 cm, what is the height?(*Give the answer correct to the nearest 0.1 cm.*)

- 16. The size of each interior angle, *I*, of an *n*-sided regular polygon can be obtained by the formula  $I = \frac{(n-2) \times 180^{\circ}}{n}$ .
  - (a) Make *n* the subject of the formula.
  - (b) How many sides does a regular polygon have if each of its interior angles is 120°?



Prove that the following pairs of triangles are congruent. [Nos. 3-4]



Determine which two triangles must be congruent and give a reason to explain your answer.



Find the unknowns in each of the following pairs of similar triangles. **[Nos. 6-7]** 



Prove that the following pairs of triangles are similar. [Nos. 8-9] 8. **z** 9.



**10.** In the figure, *CDA* and *CEB* are straight lines. Prove that  $\triangle ABC \sim \triangle DEC$ .



Multiple Choice Question

| 11. | 12. | 13. |
|-----|-----|-----|
| 14. | 15. | 16. |

**11.** In the figure,  $\triangle ABC \cong \triangle EFD$ . Which of the following must be true?



**12.** In the figure,  $\triangle PQR \cong \triangle STR$ . Which of the following may not be true?



- $\mathbf{C.} \quad PR = SR$
- **D.** QR = ST

**13.** In the figure,  $\triangle ABC \sim \triangle XZY$ . Find *AB* and *YZ*.



- **C.** AB = 27 cm, YZ = 20 cm
- **D.** AB = 27 cm, YZ = 30 cm
- **14.** It is given that  $\triangle ABC \sim \triangle RQP$ . AB = 10, PQ = 20 and 5AC = 2RP. Which of the following must be true?
  - **A.** BC = 8, QR = 4
  - **B.** BC = 8, QR = 25
  - **C.** BC = 50, QR = 4
  - **D.** BC = 50, QR = 25

**15.** In the figure, *BPC* is a straight line.



Which of the following must be true?

- I. $\triangle ABC \sim \triangle PAC$ II. $\triangle ABC \sim \triangle PBA$ III. $\triangle PAC \sim \triangle PBA$ A.I onlyC.General conduction only
- **B.** I and III only **D.** I, II and III





Which of the following must be true?

- I.  $\triangle ABD \cong \triangle BCE$
- II.  $\triangle ABD \sim \triangle FBE$
- III.  $\triangle ADB \sim \triangle FBC$

Α.

- I only **C.** II only
- **B.** I and II only **D.** I, II and III

#### Level 2

**17.** In the figure, AC and BD intersect at E. It is given that AD = BC and AC = BD.

- (a) Prove that  $\triangle ABD \cong \triangle BAC$ .
- **(b)** If  $\angle ABD = 32^\circ$ , find  $\angle DEC$ .



- **18.** In the figure, *ADC* is a straight line and  $\angle ABC = \angle BDC = 90^{\circ}$ .
  - (a) Prove that  $\triangle ABC \sim \triangle BDC$ .
  - **(b)** Prove that  $BC^2 = AC \times DC$ .



# SKH St. Simon's Lui Ming Choi Secondary School F2 Mathematics Tiered Assignment Chapter 9 linear equation in 2 unknowns

Name :\_\_\_\_\_ Class :\_\_\_\_( )

Date:

#### Tier 1

Solve the following simultaneous equation in 2 unknowns.

**1.**  $\begin{cases} y = x \\ 4x + y = 15 \end{cases}$  **2.**  $\begin{cases} 7y - x = -8 \\ x = 3y \end{cases}$ 

**3.** 
$$\begin{cases} x = -2y \\ x + 3y - 5 = 0 \end{cases}$$
**4.** 
$$\begin{cases} y = 5x - 2 \\ x = y + 6 \end{cases}$$

**5.** 
$$\begin{cases} x - y = -8 \\ x + y = 4 \end{cases}$$
 **6.** 
$$\begin{cases} 3x + 2y = -3 \\ 3x - 2y = 9 \end{cases}$$

**7.** 
$$\begin{cases} 6x = 11 + y \\ 3x = 16 - y \end{cases}$$
**8.** 
$$\begin{cases} 2x - 5y = -12 \\ -3x + 5y = 33 \end{cases}$$

**9.** 
$$\begin{cases} b = 2a - 5\\ a + b = 7 \end{cases}$$
 **10.** 
$$\begin{cases} 2h + k = 3\\ 5h - k = -24 \end{cases}$$

**11.** 
$$\begin{cases} m = 2n - 1 \\ m = 5 - 2n \end{cases}$$
**12.** 
$$\begin{cases} a = 7b + 13 \\ 6a = 7b + 8 \end{cases}$$

**13.** The sum of two numbers is 60 and their difference is 12. Find these two numbers.

**14.** The sum of two numbers is 100 and the larger number is 3 times the smaller number. Find the smaller number.

**15.** There are some ducks and sheep on a farm. The total numbers of heads and feet for these animals are 48 and 132 respectively. How many ducks and how many sheep are there on the farm?

**16.** Solve  $\begin{cases} y = 7 - 2x \\ x = -2y - 4 \end{cases}$  **A.** x = -6, y = 5 **B.** x = -5, y = 6 **C.** x = 5, y = -6**D.** x = 6, y = -5

**17.** Solve 
$$\begin{cases} 2h - 3k = -1 \\ 3h + 2k = -34 \end{cases}^{\circ}$$
  
**A.**  $h = -9$ ,  $k = -6$   
**B.**  $h = -8$ ,  $k = -5$   
**C.**  $h = -7$ ,  $k = -5$   
**D.**  $h = -6$ ,  $k = -4$ 

- **18.** The total price of 2 pencils and 9 erasers is \$92, while the total price of 8 pencils and 3 erasers is \$104. Find the price of a pencil.
  - **A.** \$8
  - **B.** \$9
  - **C.** \$10
  - **D.** \$11
- **19.** In a bag, there are 18 prisms with 101 faces in total. If the bag contains triangular prisms and rectangular prisms only, how many triangular prisms are there?
  - **A**. 5
  - **B.** 7
  - **C.** 9
  - **D.** 11

## Tier 2

Solve the following simultaneous equations in 2 unknowns **20.** 3h + 8k + 3 = -h - 3k - 7 = -4

**21.** 
$$\begin{cases} \frac{2}{7}m = 3 - n \\ \frac{4}{7}m - 2n + 10 = 0 \end{cases}$$

**22.** Sam is 5 years older than Bill. Three years later, Bill's age will be  $\frac{4}{5}$  of Sam's. How old is Bill now?

**23.** Edison is 11 years older than Ken. The age of Edison four years later will be 3 times the age of Ken three years ago. How old is Edison now?

# SKH St. Simon's Lui Ming Choi Secondary School Form 2 Mathematics Tiered Assignment Chapter 12 Trigonometric Ratios



Find the value of *x* in each of the following figures. **[Nos. 7–9]** (*Give the answers correct to 3 significant figures.*)



**10.** Find  $\theta$  in each of the following. (*Give the answers correct to the nearest* 0.1°.)

(a) 
$$9 \tan \theta = 7$$
 (b)  $\frac{1}{2} \tan \theta = 6$  (c)  $\frac{3}{4 \tan \theta} = \frac{1}{2}$ 

Find the unknown in each of the following figures. **[Nos. 11–12]** 



**13.**  $9 - 3 \tan \theta = 6$ 

 $14. \ 2\cos\,\theta = \frac{1}{\tan\,30^\circ}$ 

15. Two towers AB and MN are 100 m apart, where the height of tower AB is 18 m. A bird flies along a straight line from the roof of AB to the roof of MN, which makes an angle of 16° with the horizontal. What is the height of tower MN?

